The near wall effect of synthetic jets in a boundary layer

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Abstract

An experimental investigation to analyse the qualitative near wall effect of synthetic jets in a laminar boundary layer has been undertaken for the purpose of identifying the types of vortical structures likely to have delayed separation on a 2D circular cylinder model described in this paper. In the first instance, dye visualisation of the synthetic jet was facilitated in conjunction with a stereoscopic imaging system to provide a unique quasi three-dimensional identification of the vortical structures. Secondly, the impact of synthetic jet structures along the wall was analysed using a thermochromic liquid crystal-based convective heat transfer sensing system in which, liquid crystals change colour in response to the thermal footprints of a passing flow structure. Of the different vortical structures produced as a result of varying actuator operating and freestream conditions, the footprints of hairpin vortices and stretched vortex rings revealed a marked similarity with the oil flow pattern of a vortex pair interacting with the separation line on the cylinder hence suggesting that either of these structures was responsible in delaying separation. Conditions were established for the formation of the different synthetic jet structures in non-dimensional parameter space.
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Keywords: Synthetic jets; Boundary layer; Flow separation control; Vortex structures

1. Introduction

Synthetic jet actuators (SJA) provide a novel means of applying flow control and their potential application for the effective delay of boundary layer separation on aircraft has been the focus of intense research in recent years (Smith and Glezer, 1998; Crook and Wood, 2001; Gilarranz and Rediniotis, 2001; Glezer and Amitay, 2002). One of the reasons for this is due to their unique ability to impart additional momentum on a fluid region from which it was originally synthesised without a net mass addition, therefore requiring no bleed air supply and complex piping. In addition, the oscillatory nature of synthetic jets has been observed to offer greater entrainment of fluid in the near field compared to their continuous counterparts (James et al., 1996; Cater and Soria, 2002).

It is believed that the interaction of the discrete trains of vortices formed out of a SJA (Fig. 1) with a local boundary layer produces streamwise vortical structures, which are capable of delaying flow separation by entraining faster moving fluid from the freestream to the near wall region. Crook and Wood (2001) investigated the flow control effectiveness of an array of SJAs implemented flush to the surface of a circular cylinder upstream of its separation line in a turbulent boundary layer. From Fig. 2, surface oil patterns showed that with the actuators active, the separation line was pushed downstream noticeably. In particular, the oil flow revealed the footprints of a well defined streamwise vortex pair immediately downstream of each SJA orifice that appeared to persist for a long distance downstream and interact with the separated flow. Subsequent dye visualisation by Zhong et al. (2005) has shown that the interaction between a synthetic jet and a boundary layer is complex, varying from hairpin vortices that remain near to the wall to tilted vortex rings that penetrate the boundary layer as the jet-to-freestream velocity ratio increases. It

Nomenclature

c_f	skin friction coefficient
d	boundary layer thickness to orifice diameter ratio
D	diameter of cavity or orifice, mm
f	diaphragm oscillation frequency, Hz
h	orifice depth, mm
H	cavity height, mm
L	dimensionless stroke length
Re	Reynolds number
S	Stokes number
St	Strouhal number
T	time period of a diaphragm oscillation cycle, s
u	instantaneous velocity, m/s
U	characteristic velocity, m/s
VR	jet-to-freestream velocity ratio
x	streamwise distance from orifice exit, mm
y	normal distance from orifice exit, mm

Greek symbols

Γ	vortex circulation, m²/s
δ	boundary layer thickness, mm
Δ	peak-to-peak displacement at the diaphragm centre, mm
ρ	fluid density, kg/m³
τ	surface shear stress, N/m²
v	molecular kinematic viscosity, m²/s

Superscripts

–	time average
~	space average

Subscripts

c	cavity value
j	jet value
o	orifice value
w	wall value
∞	freestream value

Fig. 1. Schematic of a SJA.

Fig. 2. Demonstration of flow separation control (Crook and Wood, 2001).

has been hypothesised (Zhong et al., 2005) that the hairpin vortices may have been responsible for the formation of the streamwise vortex pair that interacted with the separation line on the circular cylinder, however, further evidence is still to be sought.

In this paper, the results of a qualitative study of the interaction of a synthetic jet with the near wall region of a laminar boundary layer are presented. As a continuation of the aforementioned investigation, the purpose of the work described herein is to identify the likely type of vortical structures responsible for the delayed separation on the circular cylinder and to establish the conditions that ensure the formation of such structures in non-dimensional parameter space. To this end, the nature of vortical structures produced under a range of actuator and freestream conditions are to be investigated with a view to analysing their respective near wall effects where flow control is ultimately desired. The use of a laminar flow provides a logical first step into visualising and understanding the basic mechanism of synthetic jet boundary layer interaction, which would otherwise be difficult to achieve for a turbulent boundary layer. Furthermore, it is believed by the authors that the type of vortical structures produced should essentially be the same as that for a synthetic jet issuing into a turbulent flow with the main difference being in the dissipation rate of the ejected structures near the wall. This study is therefore applicable to turbulent flows, as in the case of the cylinder model described herein.

Realisation of the aims of this study is to be made primarliy through the application of two qualitative visualisation techniques, which are novel to this area of research. In the first instance, dye visualisation of the synthetic jet structures was facilitated in conjunction with a stereoscopic imaging system to allow simultaneous side and surface views. The technique provides a unique quasi three-dimensional identification of the vortical structures produced by the synthetic jet. Secondly, the impact of

synthetic jet structures along the wall was analysed using a thermochromic liquid crystal-based convective heat transfer sensing system. Essentially, the liquid crystals change colour in response to the thermal footprints of a flow structure which causes a localised variation of convective heat transfer. The system, similar to that described by Zhong et al. (2000) therefore allows the resident effect of synthetic jets at the wall to be examined where effective flow control is ultimately desired. Collectively, the techniques will provide invaluable insights into both surface and off-surface behaviour related to synthetic jet boundary layer interaction.

2. The effect of dimensionless parameters on the characteristics of a round synthetic jet

2.1. SJA in quiescent conditions

Smith and Glezer (1998) have shown that for a SJA of a given geometry in quiescent conditions, two independent dimensionless parameters defined using the jet velocity, namely the dimensionless stroke length L and the jet Reynolds number Re_j characterise the synthetic jet flow. According to the slug model (Glezer, 1988) the stroke length L_o represents the length of the fluid column expelled during the blowing stroke, i.e.,

$$L = \frac{L_o}{D_o} = \frac{\overline{U}_o}{fD_o} \tag{1}$$

where $\overline{U}_o$ is the time-averaged blowing velocity over the entire cycle, which was originally proposed by Smith and Glezer (1998) to facilitate a comparison between synthetic jets and steady jets. For the present study

$$\overline{U}_o = \frac{1}{T} \int_0^{T/2} \tilde{u}_o(t)\,dt = \frac{1}{3} f \Delta \left(\frac{D_c}{D_o}\right)^2 \tag{2}$$

where $\tilde{u}_o(t)$ is the instantaneous space-averaged velocity at the orifice exit. Note that from the definition proposed by Smith and Glezer (1998), $\overline{U}_o$ is neither the time average of $\tilde{u}_o(t)$ over a whole cycle T, which should be zero, nor its time average over half a cycle $T/2$ (i.e., the blowing half of a cycle), which is $2\overline{U}_o$. Assuming an incompressible flow, Eq. (2) derived by Tang and Zhong (2006) equates the instantaneous volume flow rate displaced by the diaphragm with that expelled through the orifice (where the coefficient has been modified to 1/3 to account for the use of a rubber diaphragm in the present investigation). The jet Reynolds number is defined as

$$Re_j = \frac{\overline{U}_o D_o}{v} \tag{3}$$

A previous study of synthetic jets in quiescent conditions undertaken by the authors (Jabbal et al., 2006) has shown that the Reynolds number based on the stroke length, Re_L, (where $Re_L = Re_j \cdot L$) is directly related to the synthetic jet

vortex circulation, Γ/v and as such, is a more useful indicator of the vortex strength.

From these two key parameters a third dependent parameter, the Stokes number, S, which is also important can be defined accordingly

$$S = \left(\frac{2\pi Re_L}{L^2}\right)^{1/2} \tag{4}$$

2.2. SJA in a cross flow boundary layer

If the SJA is embedded in a crossflow boundary layer, the list of physical parameters on which the nature of the synthetic jet will depend should be extended to include the local boundary layer thickness δ, the freestream velocity U_∞ and the local wall shear stress τ_w. Dimensional analysis gives the following

$$\pi_1 = \frac{fD_0}{U_\infty}, \quad \pi_2 = \frac{U_\infty \delta}{v}, \quad \pi_3 = \frac{\delta}{D_0},$$
$$\pi_4 = \frac{\tau_w}{\rho U_\infty^2}, \quad \pi_5 = \frac{\overline{U}_o}{U_\infty} \tag{5}$$

where π_1 represents the Strouhal number, St, π_2 the freestream Reynolds number, Re_δ, π_3 the ratio of boundary layer thickness to orifice diameter, d, π_4 the non-dimensional shear stress (which is equivalent to the skin friction coefficient, $c_f = \tau_w/0.5\rho U_\infty^2$) and π_5 the jet-to-freestream velocity ratio, VR.

Combined with the key dimensionless parameters for a SJA in quiescent conditions, that is L and Re_L, there is a total of 7 dimensionless parameters. Taking the interdependencies of Eqs. 6(a) and 6(b) into account effectively reduces the number of parameters pertaining to a synthetic jet in a boundary layer to 5, namely L, Re_L, VR, d and c_f

$$St = \frac{VR}{L} \tag{6a}$$

$$Re_\delta = \frac{Re_L \cdot d}{L \cdot VR} \tag{6b}$$

2.3. Discussion on the effect of the dimensionless parameters

Holman et al. (2005) and Milanovic and Zaman (2005) have shown that there is a threshold of the stroke length for synthetic jet formation, for which L is approximately 0.5 for round synthetic jets in the absence of a crossflow. As such, jet formation and the ensuing injection of vorticity within the boundary layer to promote fluid mixing requires that the stroke length is larger than a critical value. The magnitude of the stroke length also determines the impact from the suction stroke, with a greater influence of suction being asserted on synthetic jets that are formed at low values of L (i.e., those in which the vortical structures have not moved sufficiently far away from the orifice during the blowing stroke). For a synthetic jet issuing into a boundary layer, it is expected that the effect of suction would be con-

fined to the upstream branch of the vortex hence resulting in an asymmetric structure. Furthermore, extensive investigations by Gharib et al. (1998) of the formation of vortex rings generated through piston-driven jets has shown that the flow field generated by large stroke lengths consist of a leading vortex ring followed by a trailing jet. Alternatively, flow fields generated by small stroke lengths show only a single vortex ring. The transition between these two states is observed to occur at a stroke length of approximately 4, thus representing the threshold of the stroke length above which, shedding of secondary vortices occurs due to saturation of vortex circulation within the primary structure. This threshold for round synthetic jets formed in quiescent conditions has also been found to occur at $L = 4$ (Jabbal et al., 2006).

It can be expected that the jet Reynolds number will have an influence on the strength of the vortical structures formed out of the orifice. A previous study by Zhong et al. (2005) of the behaviour of synthetic jets in a laminar boundary layer has characterised the Reynolds number according to the stroke length, Re_L, as defined previously. It is believed that the use of Re_L is suitable in quantifying the strength of a vortex ring and is therefore an important quantity where fluid entrainment and mixing in the near wall region via the generation of coherent vorticity is ultimately required. Nevertheless, a prerequisite to vortex strength is that of vortex roll up, which is determined by the Stokes number. It has been shown by Guo and Zhong (2006) that the Stokes number (Eq. (4)) should be >10 to ensure roll up for $L < 4$.

The velocity ratio represents the relative strength between the jet and freestream velocity and characterises the trajectory of the jet through the boundary layer. Milanovic and Zaman (2005) have previously shown that at a given streamwise location, the jet penetration height is solely a function of the momentum flux ratio, which is equivalent to the velocity ratio VR, defined in the present study. Thus at low values of VR, the synthetic jet will reside within the boundary layer for a longer period of time, thereby increasing its potential effectiveness where flow control is ultimately desired. Zhong et al. (2005) has shown that shear in the boundary layer will have a greater influence on those structures formed at low VR causing vortex stretching, as opposed to those formed at high VR. It is worth noting that the level of shear is directly related to the relative size of the boundary layer thickness to the orifice diameter, d and therefore for different d, the magnitude of VR should be set accordingly to ensure the trajectory of the synthetic jet remains in the near wall region.

Finally, the skin friction coefficient along the wall, c_f, is expected to affect the streamwise decay of the vortical structures downstream of the orifice, with the rate of vortex dissipation being greater for a higher skin friction (and therefore a higher wall friction velocity). This has particular implications for a synthetic jet embedded in a turbulent flow and will accordingly require augmentation of L, Re_L

and VR to ensure similar levels of effectiveness as a synthetic jet in a laminar flow.

Based on the aforementioned discussion, for a SJA of a given geometry embedded in a boundary layer

$$\text{SJA effectiveness} = fn(L, VR, d, Re_L, c_f) \qquad (7)$$

where effectiveness is defined as the strength and persistence of fully formed vortical structures in the near wall region of a boundary layer. The functional dependence of the effectiveness of a synthetic jet on the dimensionless parameters given in Eq. (7) also correlates with a scaling law derived by Raju et al. (2005). Using a non-linear regression analysis on data obtained by numerical simulation, a scaling law for the vorticity flux of a synthetic jet was extracted for the case of a zero-pressure gradient laminar boundary layer, in which the vorticity is influenced by a Strouhal number based on the jet velocity (equivalent to L in the present study), a jet to freestream velocity ratio, a boundary layer thickness to slot width ratio and a jet Reynolds number. The scaling law shows that for a constant boundary layer thickness, the vorticity flux of a synthetic jet embedded in a boundary layer varies with the natural logarithm of Re_j and as a linear function of L and VR^{-1}.

3. Experimental approach

Investigation of the interaction of a synthetic jet with a laminar boundary layer was conducted in a 4 m tilting water flume at the University of Manchester Goldstein Research Laboratory. The test section of the flume is approximately 0.8 m in length and has a cross-sectional area of 0.3 m × 0.3 m. The maximum freestream velocity in the test section is approximately 0.4 m/s. The SJA used in this investigation consisted of a cylindrical cavity bounded by rigid sidewalls with an orifice plate at one end and a diaphragm clamped to the other (Fig. 1). The cavity has a diameter, $D_c = 45$ mm and height, $H = 25$ mm. The orifice has a diameter, $D_o = 5$ mm and a thickness equivalent to the orifice depth, $h = 5$ mm.

3.1. Stereoscopic dye visualisation

For dye flow visualisation, the synthetic jet actuator was mounted on the back of a flat plate that formed the ceiling of the test section, as shown in Fig. 3. The plate constructed from a 5 mm thick sheet of aluminium, 1.3 m in length, was mounted horizontally and spans across the width of the test section. The plate has a 1:5 superelliptical leading edge, which according to Narasimha and Prasad
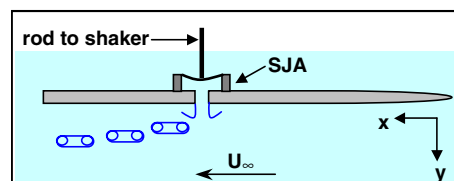

Fig. 3. Schematic sketch of test section.

(1994), helps to minimise flow separation and premature transition at the leading edge of the plate. The plate was inclined at a small negative incidence (<1°) to the oncoming flow to ensure that a fully attached laminar boundary layer forms right at the leading edge.

The SJA orifice opening was flush to the lower test surface of the plate and was located approximately 0.7 m (140 orifice diameters) aft of the leading edge. During testing, the plate and SJA cavity were both fully submerged in water. A diaphragm made from rubber was clamped to the top of the cavity and was attached at its centre via a steel rod to a permanent magnetic shaker housed above water level, which oscillates the diaphragm in a sinusoidal manner. A rubber diaphragm was used to ensure an accurate sine wave deformation, which would otherwise be difficult to achieve with a metallic one for the very low actuation frequencies and amplitudes used in the present investigation. A dye, comprising of a mixture of food colouring and methanol was introduced into the cavity via gravity.

In the experiment, a Hitachi KP-F120 partial scan CCD camera was used to capture the dye pattern produced by synthetic jets from two orthogonal views simultaneously (from the side and plane of the wall) at a frame rate of 30 fps, providing a quasi three-dimensional visualisation of the jet. To facilitate the capture of both views simultaneously onto each image frame, a stereoscopic imaging sys-

tem, as shown in Fig. 4, was set up using a combination of two plane mirrors and an orthogonal prism in accordance with the method described by Zhang et al. (2003).

3.2. Liquid crystal visualisation

For liquid crystal visualisation, the aluminium plate was replaced with a 10 mm thick Perspex plate of the same length and width. The plate leading edge profile, incidence of the plate to the oncoming flow and SJA orifice location aft of the leading edge were consistent with those for the dye flow tests. A 500 mm × 250 mm cavity was cut out of the downstream half of the plate to accommodate a heater composite insert.

The composite is essentially a flat plate composed of several layers, as shown in Fig. 5a. The heater is a resistive wire-wound element encased in silicone rubber and is designed to give a uniform heat capacity to a maximum of 1.7 kW. A 3 mm thick aluminium sheet is attached to the heater to smooth out any lateral temperature nonuniformity caused by the wire element. A black high impact polystyrene sheet 0.5 mm thick is bonded to the aluminium and has the opposite effect, in that it minimises lateral heat conduction along the surface thereby helping to retain the localised effect of temperature non-uniformity associated with the thermal footprints of a synthetic jet. The different layers of the composite are bonded together using a double-sided 3M adhesive tape to ensure good thermal contact and the composite is inserted into the cavity so that the polystyrene sheet is flush to the lower test surface of the Perspex plate. To minimise heat losses through the back of the composite, a 5 mm air gap is sealed above the heater using a Perspex lid. A 5 mm hole constitutes the SJA orifice through the composite, which has a total thickness equivalent to the orifice depth, h of 5 mm. The SJA cavity is mounted on the back of the composite on the surface of the heater.

A temperature-sensitive liquid crystal layer of approximately 50 μm was applied on the polystyrene surface using an airbrush. A single coating of a binder (Hallcrest AQB-3) was applied on top of the liquid crystal layer and acts as a varnish to protect it from water. The liquid crystal used is BM/R22C5W supplied by Hallcrest and has an active colour bandwidth of 5 °C, showing red at 22 °C and blue at 27 °C (tolerances of quoted temperatures are ± 1 °C). In
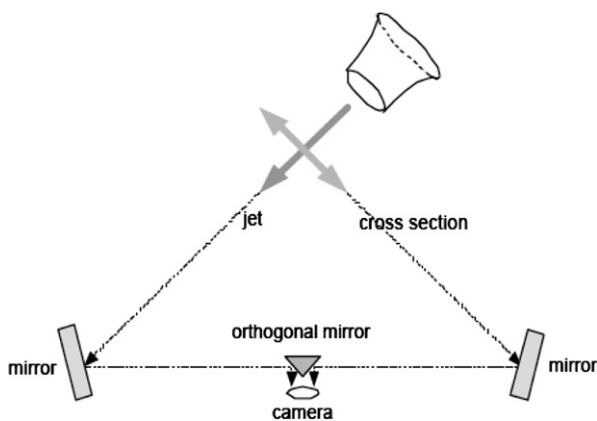
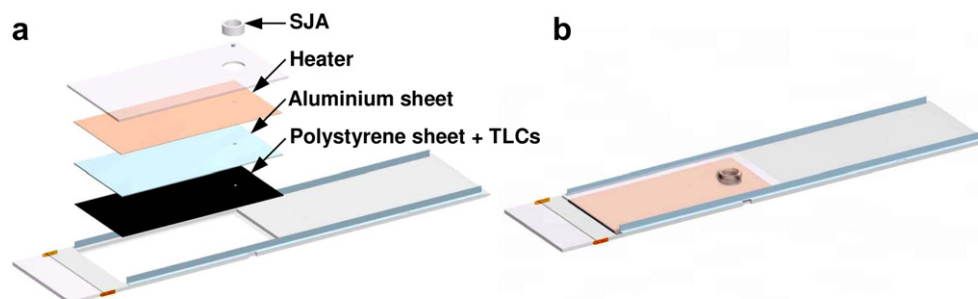Fig. 4. Stereoscopic viewing system for dye visualisation (Zhang et al., 2003).

Fig. 5. (a) Modular construction of flat plate embedded with heat transfer sensing system and (b) plate in its complete form.

the experiment, the surface is heated to such an extent that the crystal shows blue colour under a laminar boundary layer. As the synthetic jet passes, its thermal footprint can be seen by a change in colour through the spectrum to red. The thermal footprints were captured with a standard colour video camera.

3.3. Test conditions

In the present investigation, the non-dimensional flow characteristics of the synthetic jet were varied by changing the diaphragm operating conditions (oscillation frequency, f and peak-to-peak displacement, Δ) and freestream conditions (namely, the freestream velocity, U_∞). A LabVIEW virtual instrument was used for signal generation of a sinusoidal waveform at a specified diaphragm oscillation frequency, which was sent to the permanent magnetic shaker via an ADC device. The diaphragm displacement was measured using an eddy current displacement sensor and read into the virtual instrument. The time-averaged blowing velocity over the entire cycle was evaluated from Eq. (2), which is applicable for incompressible flows. Eq. (2) was validated from hotwire measurements by Li and Zhong (2005) with an uncertainty of 9.7% between the theoretical and measured value of $\overline{U}_o$.

The freestream velocity was measured using a Nixon Streamflo 403 vane anemometer, which has an accuracy of ±2% of the flow velocity. The undisturbed boundary layer velocity profiles were measured using PIV. To facilitate measurements, the freestream flow was seeded with hollow glass particles with a mean diameter of 10 μm and a density of 1100 kg/m^3. The settling velocity of the particles is approximately 5 μm/s thus suggesting that the particles will follow the motion of the flow with high fidelity. The accuracy of the PIV measurements was assessed from continuity in accordance with the method outlined by Chang et al., 2001, which yielded a maximum uncertainty of 4.8%. A light sheet approximately 1 mm in width was generated by a 5 W Argon ion laser to illuminate the flow

field along a streamwise plane, which bisects the SJA orifice along its centreline. A Photron Ultima APX camera with a resolution of 1024×1024 pixels was used to capture images in a field of view of 25 mm × 25 mm. Corresponding vectors were resolved using a two-frame cross-correlation algorithm in which, a 32×32 pixel interrogation area with an overlap ratio of 50% was chosen giving a spatial separation between adjacent vectors of 0.39 mm. Long time-averaged velocity profiles were obtained over a recording time of 24 seconds. Comparison of the undisturbed boundary layer velocity profile with the Blasius solution at $U_\infty = 0.05$ m/s and $U_\infty = 0.1$ m/s along a streamwise centreline location at 5 orifice diameters upstream of the orifice is shown in Fig. 6. The good agreement confirms the zero-pressure gradient nature of the laminar boundary layer.

A summary of all the test cases is shown in Table 1. The dimensionless stroke length, L varies between 0.8 and 5.1, Reynolds number, Re_L between 16 and 658, velocity ratio, VR between 0.04 and 0.7 and Strouhal number, St between 0.05 and 0.2. For the two values of U_∞ tested, 0.05 m/s and 0.1 m/s, the respective changes in d (3.6 and 2.3) and c_f (4.13×10^{-3} and 2.65×10^{-3}) obtained from the velocity profiles in Fig. 6 were relatively small such that their effects were considered secondary to changes in the other aforementioned parameters. Thus, the focus of the parameter

Table 1
Experimental parameters

	$U_\infty = 0.05$ m/s						$U_\infty = 0.1$ m/s					
L	Re_L	VR	St	Re_L	VR	St	Re_L	VR	St	Re_L	VR	St
0.8	16	0.08		33	0.16		16	0.04		33	0.08	
1.1	29	0.11		58	0.22		29	0.05		58	0.11	
1.4	46	0.14		91	0.27		46	0.07		91	0.14	
1.9	89	0.19		179	0.38		89	0.09		179	0.19	
2.2	117	0.22	0.1	233	0.43	0.2	117	0.11	0.05	233	0.22	0.1
2.7	182	0.27		365	0.54		182	0.14		365	0.27	
3.5	308	0.35		616	0.70		308	0.18		616	0.35	
4.1	410	0.41					410	0.20				
5.1	658	0.51					658	0.26				

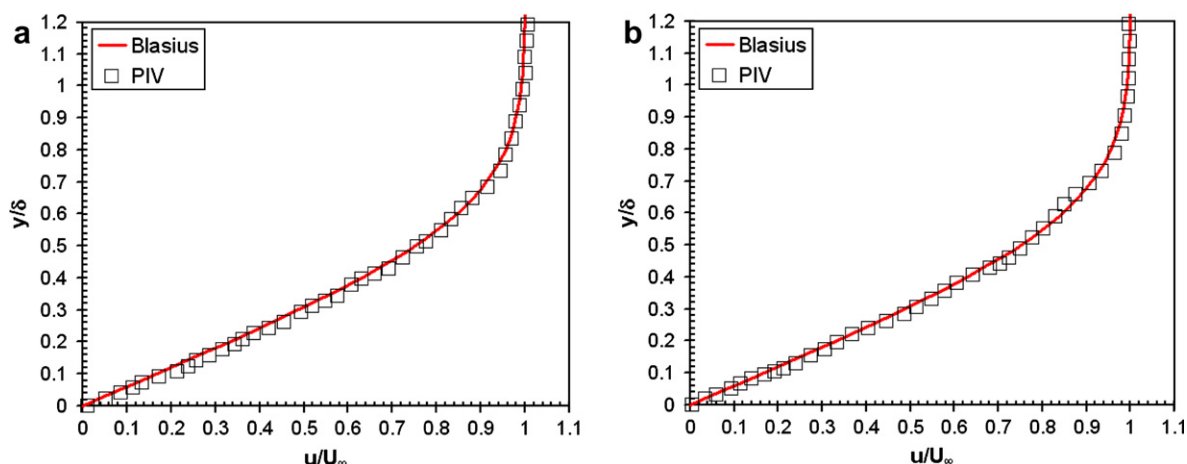

Fig. 6. Undisturbed boundary layer velocity profiles along a streamwise centreline location at $x/D_o = -5$ for (a) $U_\infty = 0.05$ m/s and (b) $U_\infty = 0.1$ m/s.

space (Eq. (7)) with respect to the results in the next section is on L, VR and Re_L.

4. Results and discussion

4.1. Near wall effect of vortical structures

In the present study, three main types of vortical structures have been identified from the interaction of a synthetic jet with a zero pressure gradient laminar boundary layer, namely hairpin vortex, stretched vortex ring and tilted/distorted vortex ring. These are similar to those observed by Zhong et al. (2005). In order to differentiate these structures by their impact on the flow in the near wall region where flow control is ultimately desired, liquid crystal images are correlated with the patterns observed by dye visualisation.

Stereoscopic dye visualisation and corresponding surface liquid crystal data of a synthetic jet produced at VR = 0.14, $Re_L = 46$ and $L = 1.4$ are shown in Fig. 7a. It can be seen from the dye visualisation that under such low VR, elongated hairpin vortices are formed out of the orifice. The structures remain embedded within the near wall region of the boundary layer on account of their low VR. As such, the level of shear in the boundary layer plays an important role in that the counter-rotating legs of the hairpins experience significant stretching as they propagate downstream. This is represented by the trace of the structure as seen with the dye, which appears as a thin line thus suggesting that the vortex tube is highly stretched. It may also be observed from both side and surface views that the counter-rotating legs of the hairpins can be traced back to the orifice from which they were formed, suggesting that the suction stroke is dominant for this type of structure (equating to a small stroke length). In addition to the hairpin structures, the surface view shows the development of two dye concentrations, which appear laterally to either side of the dark concentration created by the counter-rotating legs of the hairpin vortices.

Similar observations were made by Acarlar and Smith (1987) in their study of hairpin vortices in a laminar boundary layer, where the dye concentrations were shown to be a secondary or longitudinal vortex pair not too dissimilar to the horseshoe-type vortex observed to form at end wall junctures. The formation of the longitudinal vortex pair is characteristic of hairpin vortices formed at low injection rates, or as in this case, low VR and are created by the inrush of fluid outboard of the counter-rotating hairpin legs.

Due to the weak nature of the structures caused by a low Re_L, their ability to affect the near wall region appears limited, as confirmed by the corresponding liquid crystal image (however, one also needs to consider the development of the thermal boundary layer along the wall, which results in an increasing surface temperature downstream, thereby making it more difficult to differentiate the thermal footprints with downstream distance).

Within $6D_o$ of the orifice there appears three dark (red) streaks representing a drop in the local surface temperature due to a relatively high level of convective heat transfer associated with the passing structures. By Reynolds analogy, a local increase in heat transfer correlates to a local increase in fluid momentum. The two outer streaks are associated with the counter-rotating legs of the hairpins, which have 'common flow' upwards such that higher momentum fluid is brought towards the wall outboard of the legs. Conversely, the centre streak is associated with the longitudinal vortices, which have 'common flow' downwards (as shown by Acarlar and Smith, 1987) and from Fig. 7a are seen to form inboard of the hairpin vortex within $4D_o$ of the orifice (note the two dye lines pertaining to the longitudinal vortices in between the hairpin legs in the near field region). Hence higher momentum fluid is brought towards the wall inboard of the longitudinal vortices resulting in a higher heat transfer region.

Fig. 7b shows the formation and advection of hairpin vortices at VR = 0.19, $Re_L = 89$ and $L = 1.9$. Due to an increase in Re_L, the strength of the hairpins appear greater than those in Fig. 7a, as evidently shown by the vortex tube pertaining to the head and legs of the structure. It is also observed that the longitudinal vortices have completely diminished. Both types of hairpin vortices with and without the longitudinal vortices are collectively grouped as 'hairpin vortices' since the presence of a hairpin vortex is the dominant feature in both cases.

Fig. 8a shows the corresponding development of the hairpin vortex as it is formed out of the orifice. The vortical structure produced by the synthetic jet is seen to experience an asymmetric roll up, similar to the findings of Zhong et al. (2005). Since the dimensionless stroke, L, for this case is quite small, the structure does not move sufficiently far from the orifice before the suction stroke begins. Consequently, the onset of suction weakens roll up on the upstream side whilst the downstream branch is strengthened by the vorticity in the boundary layer thereby resulting in an asymmetric structure. It is therefore evident that suction influences the formation of this structure. The stereoscopic dye image also reveals that the counter-rotating legs of successive hairpins are connected with each other and are traceable back to the orifice exit.

As the structures move downstream, as well as experiencing a high degree of stretching, the heads undergo a lifting movement from the wall due to self induction. It is found that the hairpin structures produce two streamwise streaks of high heat transfer that persist downstream. As in Fig. 7a, the nature of these footprints can be attributed to the counter-rotating legs. As the legs of the hairpins rotate, low momentum fluid adjacent to the wall accumulates between them generating a region of low heat transfer (corresponding to the light (blue)[1] region between the

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[1] For interpretation of the references to colour in this figure, the reader is referred to the web version of this article.
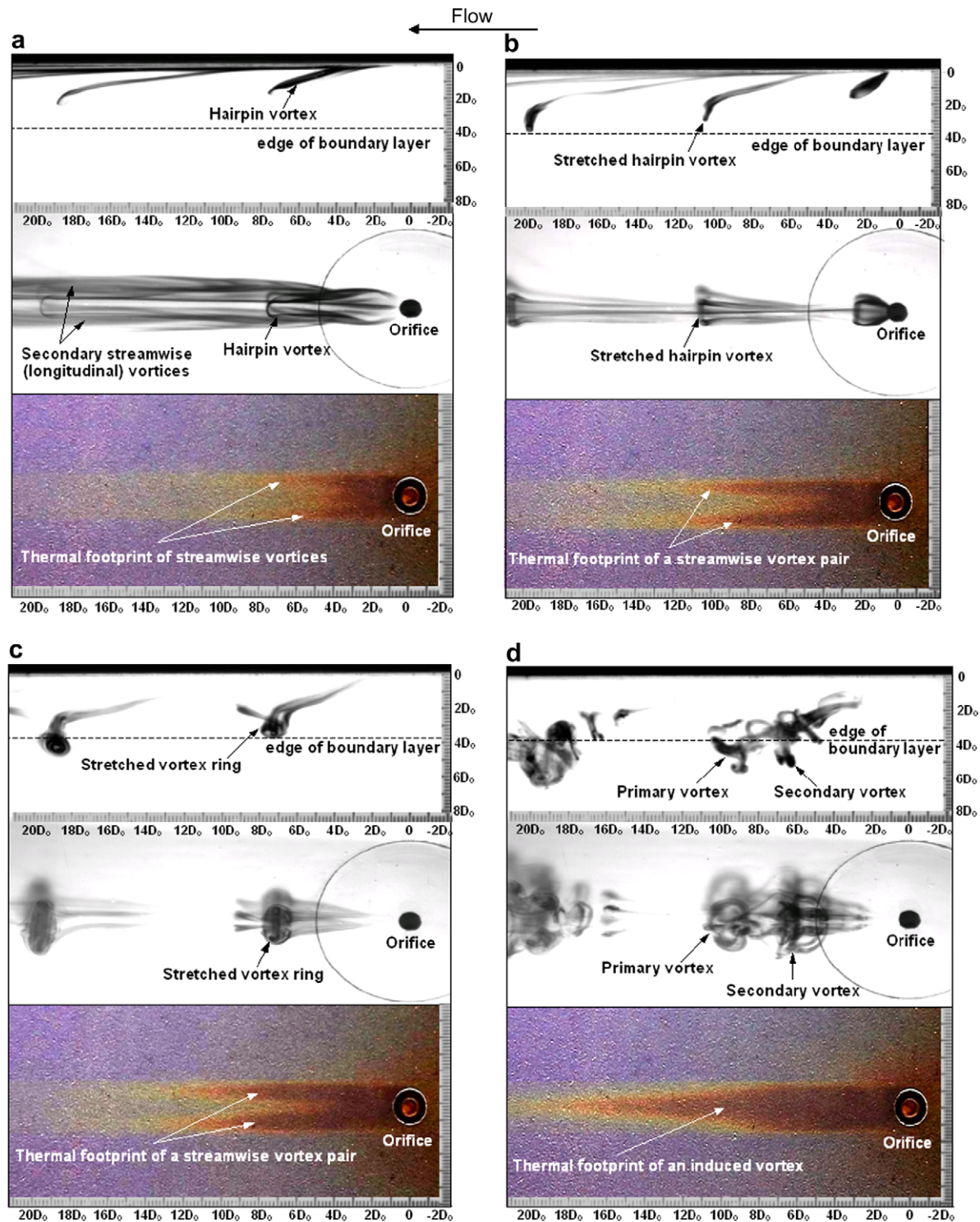
Fig. 7. Stereoscopic dye and surface liquid crystal images of a synthetic jet at (a) $VR = 0.14$, $Re_L = 46$ and $L = 1.4$, (b) $VR = 0.19$, $Re_L = 89$ and $L = 1.9$, (c) $VR = 0.27$, $Re_L = 182$ and $L = 2.7$ and (d) $VR = 0.51$, $Re_L = 658$ and $L = 5.1 - St = 0.1$ and $d \approx 4$ for all cases.

streamwise streaks). Outboard of the legs, higher momentum fluid is brought towards the wall, thereby generating two streamwise regions of high heat transfer that correspond to the dark (red) streaks produced by the liquid crystal.

Fig. 7c shows the formation and advection of a stretched vortex ring at $VR = 0.27$, $Re_L = 182$ and $L = 2.7$. Similarly, a close-up development of the structure out of the orifice is shown in Fig. 8b. A rollup on the upstream side of the vortex is observed, which is significantly weakened
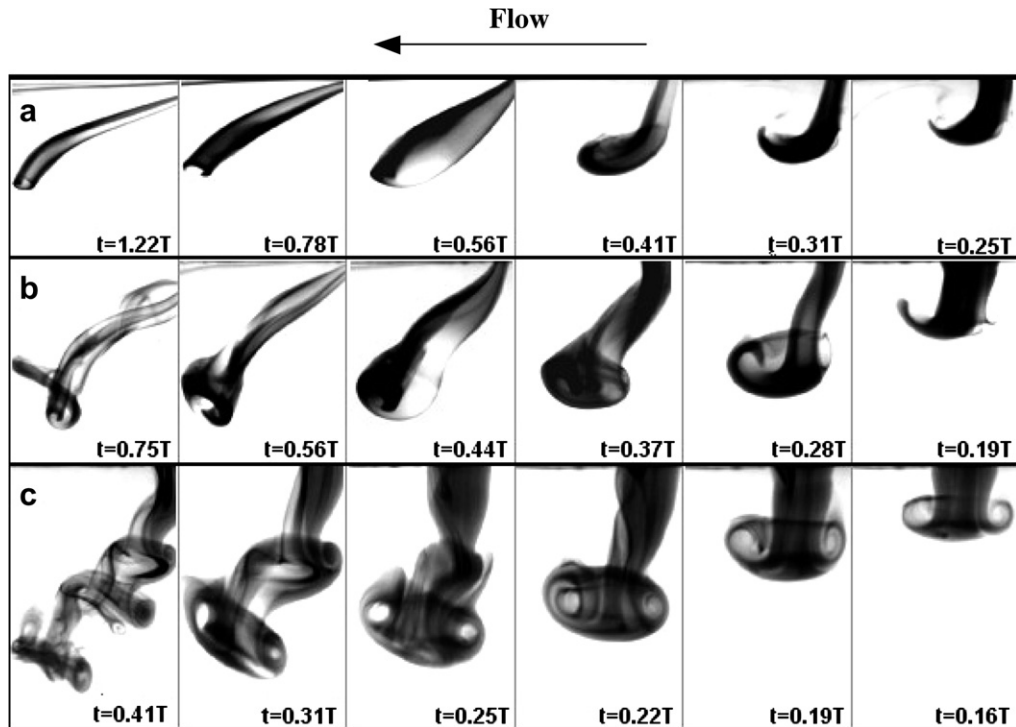
Fig. 8. Close-up view of synthetic jet formation and roll up for (a) hairpin vortices, (b) stretched vortex rings and (c) distorted vortex rings.

by the vorticity in the boundary layer. Conversely, the strength of the downstream branch becomes intensified due to stretching. Anticlockwise tilting is also evident by the motion of the vortex head as the structure convects downstream. Based on the spinning solid cylinder concept suggested by Chang and Vakili (1995), Zhong et al. (2005) attributes this behaviour to the moment of the Magnus forces acting on the vortex rollers. The structure as shown by the dye pattern differs from the hairpin vortices in two ways. Firstly, the vortex rollers in the head of the structure are more prevalent (as shown in Figs. 7c and 8b), which may be attributed to an increase in Re_L. Secondly, the counter-rotating legs of the structure detach away from the wall and also from the orifice, suggesting that for this stroke length of $L = 2.7$, the effect of suction is minimal. Further observations show that the structures have a steeper trajectory than the hairpin vortices on account of their higher VR, which causes the structures to eventually penetrate out of the boundary layer.

Nevertheless, the near wall effect of these structures is qualitatively very similar to that which is observed for the hairpins, since the counter-rotating legs still sweep over the wall due to a degree of tilting. Two streamwise streaks of high heat transfer produced by the counter-rotating legs are evident. Close observation reveals the width of these streamwise streaks is slightly greater than those produced by the hairpins. This could be attributed to the higher strength of the stretched vortex rings. Moreover, since the stretched vortex rings are stronger and further away from the wall, the counter-rotating legs bring in higher momentum fluid from the surroundings than those of the

hairpin vortices, thereby resulting in an increased rate of heat transfer along the wall. As in the work of Zhong et al. (2005), this type of structure is regarded as an intermediate case between those structures than remain embedded in the boundary layer, as previously described and those that rapidly penetrate it, as described below.

Fig. 7d shows the advection of a distorted vortex ring out of the boundary layer (where VR = 0.51, $Re_L = 658$ and $L = 5.1$). The formation of the structure out of the orifice (Fig. 8c) shows that it initially experiences a symmetrical roll up, since the strength of the jet is increased relative to the freestream, with the ensuing vortical structure penetrating the boundary layer. Consequently, boundary layer shear has little influence on this structure unlike the previous cases, which experience a large degree of stretching due to their long resident time in the boundary layer. The structure, as shown in Fig. 8c becomes increasingly incoherent with time and the formation of secondary vortices can eventually be seen shedding from the primary vortex ring. The formation of these secondary vortices indicates that a limit in the circulation that can be contained within the primary vortex has been reached. For this case, the dimensionless stroke length is above the threshold of $L = 4$ for the shedding of secondary vortices found for synthetic jets in quiescent conditions (Jabbal et al., 2006).

The corresponding thermal footprint produced by the distorted vortex ring is distinctly different to those observed for the hairpin vortices and stretched vortex rings. In this case, there is a single dark (red) streak of high heat transfer downstream of the orifice. In the case of Fig. 7d, it is hypothesised that the region of high heat transfer is pro-

duced by a tertiary vortex pair induced close to the wall by the secondary vortex of the distorted vortex ring. Since this tertiary vortex is not formed out of the orifice, it does not entrain any dye and therefore cannot be visualised. This hypothesised mechanism has recently been validated for a similar case (Jabbal and Zhong, 2007). The effect of the tertiary vortex is similar to that of the longitudinal vortices observed in Fig. 7a, having a 'common flow' downwards, thereby increasing fluid momentum and heat transfer along the centreline region. For a further increase in VR it is expected that the near wall effect of the synthetic jet will diminish.

4.2. Correlation of vortical structures to the delayed separation on a cylinder

Fig. 9 shows a magnified view of the surface oil flow pattern generated by the interaction of a synthetic jet with the separation line on a circular cylinder, as previously seen in Fig. 2. The streaklines reveal a clear footprint associated with the development of a streamwise vortex pair downstream of the SJA orifice, which interacts with the separation. A flow topology of the streaklines, as presented by Crook (2002) is included for clarity. Based on the similarity in their thermal footprints to the flow pattern revealed by the oil flow on the 2D cylinder model, it is believed that either the hairpin vortices or the highly stretched vortex rings are responsible for producing the well defined stream-
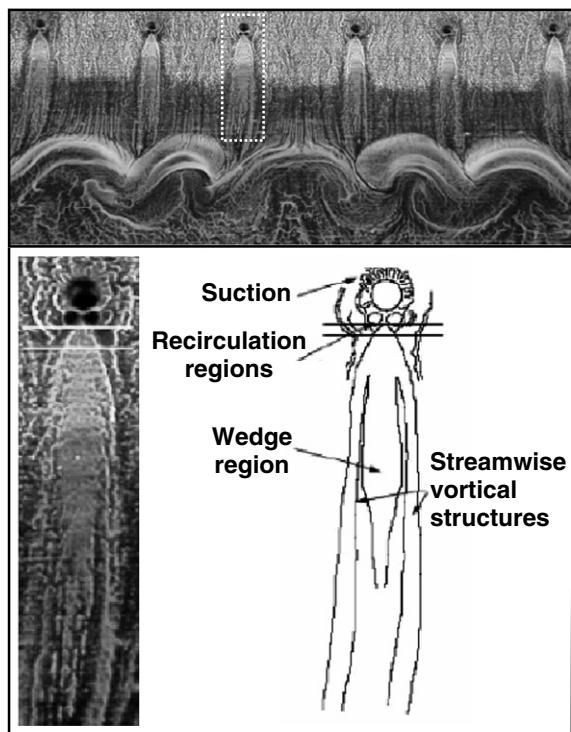

Fig. 9. Oil streaklines and corresponding flow topology of a streamwise vortex pair produced by a synthetic jet interacting with flow separation (Crook, 2002).
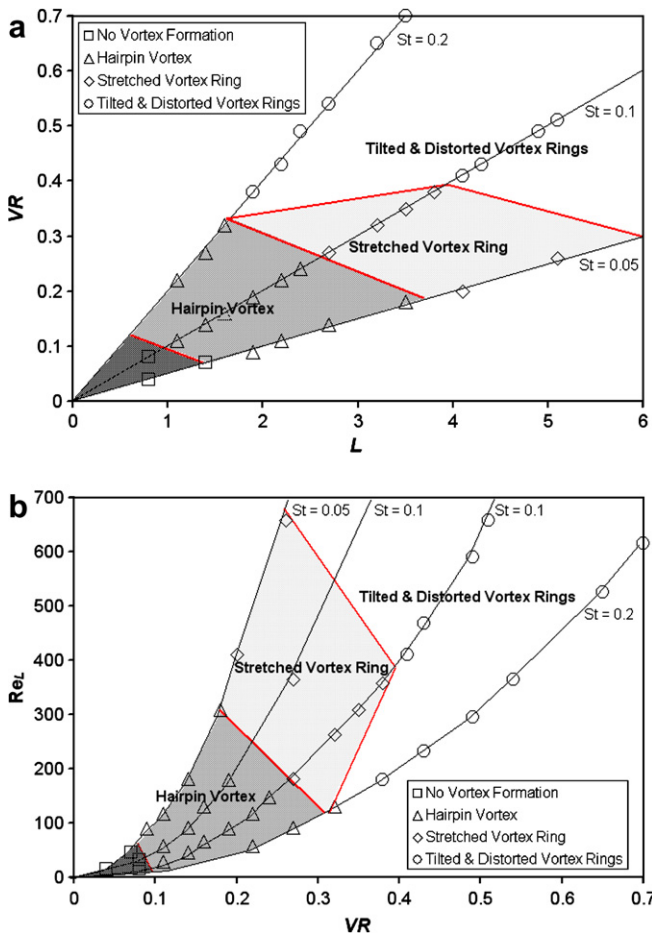
wise vortex pairs that delayed flow separation on the 2D circular cylinder.

In addition to the streamwise tracks produced by the vortex pair, the flow topology downstream of the actuator orifice reveals the presence of a wedge region embedded between the streamwise vortices. Crook (2002) offered no explanation to the cause of this wedge region. However, a possible hypothesis for the wedge may be provided from Fig. 7a in which, a third streak embedded between the two streaks of high heat transfer is observed. As previously described the middle streak, which is attributed to the 'common flow' down induced by the longitudinal vortices that initially form inboard of the hairpin legs before moving laterally outboard of them, appears to give rise to a wedge-like pattern embedded between the vortices. This hypothesis seems to lend further support to the belief that the interaction of a synthetic jet with a laminar and turbulent boundary layer is essentially the same. As such, based on their near wall persistency and similar qualitative effects along the wall, both hairpin vortices (with and without a longitudinal vortex pair) and stretched vortex rings appear potentially useful.

4.3. Parameter mapping of vortical structures

Having identified the possible types of vortical structures that were responsible in delaying flow separation on the cylinder, it is useful to establish the conditions that ensure the formation of such structures. To undertake this task, it was necessary to correlate all test cases to a parameter map based on the key dimensionless parameters of synthetic jets in a boundary layer defined according to Eq. (7). As such, the test cases shown in Table 1 were plotted as a function of L, VR and Re_L to give the two 2D graphs in Fig. 10. It is seen that the gradient of the VR–L graph shown in Fig. 10a is equivalent to the Strouhal number, St (Eq. (6a)). Fig. 10b shows the Re_L–VR graph with lines of constant St added. Note that the lines with $St = 0.1$ do not coincide with each other, as in Fig. 10a due to the different values of Re_L (also refer to Table 1 for clarity). From Fig. 10a it can be seen that there is a minimum threshold in the stroke length of $L \approx 1$ and VR ≈ 0.1, which is required for vortex formation in a boundary layer. For the vortical structures believed to be responsible for the separation delay on the cylinder, that is hairpin vortices and stretched vortex rings, there appears to be an upper limit in the velocity ratio of VR ≈ 0.4 below which, these structures are formed. Within the test conditions covered by this study, both L and Re_L do not appear to impose a similar restriction on the formation of these two types of structures. As such, Fig. 10 confirms the formation of hairpin vortices at relatively low velocity ratios of $0.1 < VR < 0.32$ since these structures remain embedded close to the wall. For stretched vortex rings, the range in VR over which these structures appear is $0.2 < VR < 0.38$. The intermediate range of VR ensures substantial resident time in the boundary layer. Finally,

Fig. 10. (a) VR–L and (b) Re_L–VR parameter space of the different vortical structures seen as a result of the interaction between a synthetic jet and a boundary layer.

for the tilted/distorted vortex rings, which are not considered to be responsible for the delayed separation on the cylinder due to their short resident time in the boundary layer and dissimilar footprints, VR > 0.38. The high threshold of VR confirms that these structures penetrate the boundary layer over a short distance downstream.

From Fig. 10 it may be seen that reducing VR for a particular type of structure results in an extension to the range of L (and hence Re_L) over which the structure is formed. This is true for both hairpin vortices and stretched vortex rings and suggests that the conditions for enhancing the flow control effectiveness of synthetic jets by the generation of vortical structures of relatively high strength that persist in the near wall region depends on limiting VR (ideally <0.4, based on the current set of cases) whilst increasing L and hence Re_L. This assessment also correlates with the previously defined scaling law derived by Raju et al. (2005), which shows that the vorticity flux of a synthetic jet embedded in a zero-pressure gradient laminar boundary layer varies as a linear function of L and VR^{-1}. In the present study for a fixed SJA geometry and given set of freestream conditions, L is a function of the peak-to-peak diaphragm displacement, Δ (Eq. (1)), Re_L a function of

the diaphragm oscillation frequency, f and Δ^2 and VR a function of f and Δ (Eq. (5)). Thus, the outlined mechanism for SJA effectiveness may be achieved by increasing Δ whilst reducing f, thereby decreasing both St and S. However, there is a compromise to be attained between reducing the actuation frequency for maximising vortex strength near the wall and ensuring a Stokes number >10 for vortex roll up at $L < 4$ (Guo and Zhong, 2006).

The dimensionless flow parameters for the synthetic jet array implemented on the cylinder model suggests that the delayed separation shown in Fig. 9 was achieved via the aforementioned route for flow control, in which St was estimated to be 0.036 (where the local external velocity of the cylinder was assumed to be twice that of the freestream), a VR of 0.25 and L approximately 7. Although this dataset is beyond the range of the parameter space shown in Fig. 10, it is anticipated that it would yield the formation of a highly stretched, streamwise-aligned hairpin vortex or stretched vortex ring. Although for a fully turbulent boundary layer, the types of synthetic jet structures formed are expected to remain as those identified, the magnitude of VR, L and Re_L at which these structures are produced are likely to shift.

5. Conclusions

An experimental investigation to obtain the qualitative near wall effect of synthetic jets in a laminar boundary layer has been undertaken for the purpose of identifying the types of vortical structures likely to have delayed separation on a 2D circular cylinder model described herein. Dye visualisation of synthetic jets in conjunction with liquid crystal visualisation along the wall was conducted for a range of actuator operating and freestream conditions. From this investigation, it has been found that

- Three types of vortical structures have been identified from the interaction of a synthetic jet with a zero pressure gradient laminar boundary layer – hairpin vortices (with and without secondary longitudinal vortices), stretched vortex rings and tilted/distorted vortex rings. These structures differ from each other primarily in terms of vorticity strength and in the time they are resident in the near wall region.
- The thermal footprints of the hairpin vortices and stretched vortex rings revealed a marked similarity with the oil flow pattern generated on a 2D circular cylinder model in terms of the wedge region and streamwise tracks, hence suggesting that either of these structures was responsible for the delayed separation on the cylinder.
- For both hairpin vortices and stretched vortex rings, there appears to be an upper limit in the jet-to-freestream velocity ratio of VR ≈ 0.4 below which, these structures are formed (hairpin vortices: 0.1 < VR < 0.32; stretched vortex rings: 0.2 < VR < 0.38 and distorted vortex rings: VR > 0.38). Within the parameter

space presented, both the dimensionless stroke length, L and Reynolds number, Re_L do not appear to impose a similar restriction on the formation of these structures.

Work has recently been undertaken to quantify the impact of synthetic jets in the near wall region of a boundary layer by utilising high frame rate streamwise PIV to provide velocity profile and wall shear stress measurements, as reported in Jabbal and Zhong (2007). It is anticipated that the findings from this research will allow for a potential identification of the vortical structure effectiveness for flow separation control.

Acknowledgements

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